How is the Minimum Wage Shaping the Wage Distribution:

Bite, Spillovers, and Wage Inequality

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Motivation

Introduction

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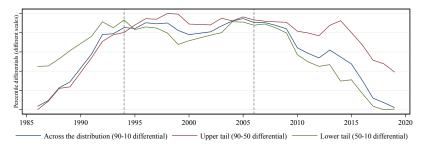
- Wage inequality rising in most advanced economies, especially at the top of the distribution
- Behavior at the bottom has been much more heterogeneous
- Negative correlation between the importance of the minimum wage and lower-tail inequality in many countries
 - US: real MW fell and lower-tail wage inequality increased (DiNardo, Fortin, and Lemieux 1996; Lee 1999)
 - UK, Germany: instituted a MW and lower-tail wage inequality decreased (Stewart 2012; Bossler and Schank 2020)
- We see that negative correlation in Portugal

Wage inequality in Portugal

Introduction

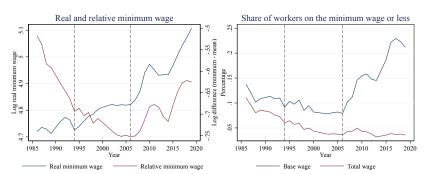
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- ▶ Rose rapidly until 1994, mainly at the top
 - Unequal returns to education (Machado and Mata 2005)
 - Increasing levels of education (Pereira 2020)
- ▶ Stabilized until mid-2000s, across the distribution
 - Fading assortative matching (Portugal, Raposo, and Reis 2018)
 - Demand for unskilled workers (Centeno and Novo 2014)
- Fell sharply since then, mainly at the bottom
 - We don't know why (gap in the literature)



Importance of the minimum wage

The importance of the minimum wage **decreased** until the mid-1990s, **was stagnant** until the mid-2000s, and **increased sharply** since then



How does the minimum wage shape the wage distribution?

Disemployment effects

- Workers that cannot find a job with the higher minimum
- Increase income inequality, but *ironically* reduce wage inequality
- Often negligible and sometimes even go in the opposite direction (Card and Krueger 1994; Portugal and Cardoso 2006)

► The minimum wage bite

- Workers that get their wages pushed up to the new minimum wage
- ▶ This is the main purpose, and the main effect, of the minimum wage (Freeman 1996; Machin, Manning, and Rahman 2003)

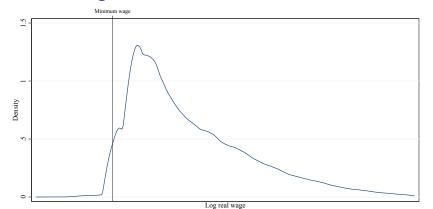
Spillover effects

- ▶ Workers that get higher wages than the new minimum
- ▶ Relative wages: firms reward more productive/skilled workers (Katz and Krueger 1992; Lee 1999; Fortin, Lemieux, and Lloyd 2021)
- Collective bargaining may play major role (Card and Cardoso 2021)

The empirical strategy

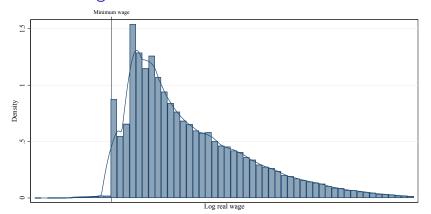
- 1. Construct the conditional wage distribution
 - Capture the minimum wage effects
- 2. Construct counterfactual distributions
 - With past minimum wage
 - Without spillovers
- 3. Quantify and decompose changes in the wage distribution

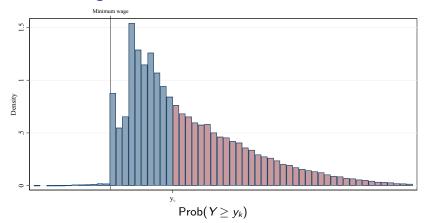
Results

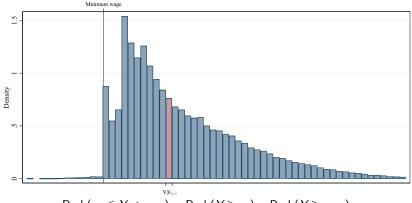


Results

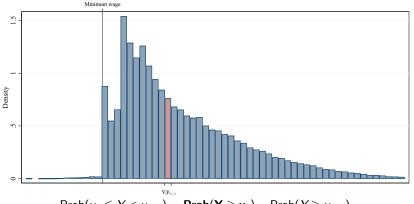
1. Constructing the conditional distribution







 $\mathsf{Prob}(y_k \leq Y < y_{k+1}) = \mathsf{Prob}(Y \geq y_k) - \mathsf{Prob}(Y \geq y_{k+1})$



$$\mathsf{Prob}(y_k \leq Y < y_{k+1}) = \mathsf{Prob}(\mathbf{Y} \geq \mathbf{y_k}) - \mathsf{Prob}(Y \geq y_{k+1})$$

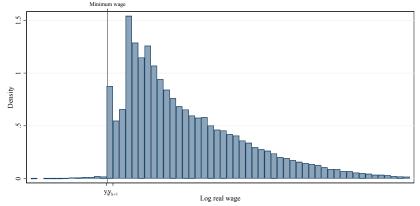
Distribution regression (Chernozhukov et al. 2013)

Prob
$$(Y > y_k) = \Phi(X\beta_k)$$

Rank regression (Fortin and Lemieux 1998) $Prob(Y > y_k) = \Phi(X\beta - c_k)$

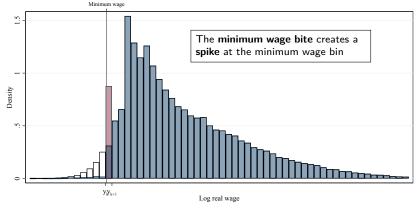
 $Prob(Y \ge y_k) = \Phi(X\beta + y_k X\gamma - c_k)$

Capturing the minimum wage effects



$$Prob(y_k \le Y < y_{k+1}) = \Phi(X\beta + y_k X\gamma - c_k) - \Phi(X\beta + y_{k+1} X\gamma - c_{k+1})$$

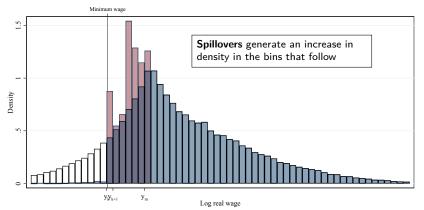
Capturing the minimum wage effects



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$$Prob(Y > y_k) = \Phi(X\beta + y_k X\gamma - c_k + \delta_0) \quad \text{for } y_k > MW_t$$

Capturing the minimum wage effects



$$Prob(y_k \le Y < y_{k+1}) = \Phi(X\beta + y_k X\gamma - c_k) - \Phi(X\beta + y_{k+1} X\gamma - c_{k+1})$$

$$Prob(Y > y_k) = \Phi(X\beta + y_k X\gamma - c_k + \delta_0 + \delta_1 + ... + \delta_m) \quad \text{for } y_m > MW_t$$

Estimating the model

$$\operatorname{Prob}(Y_{it} \geq y_k) = \Phi\left(X_{it}\beta + y_k X_{it}\gamma + \sum_{m=b}^{a} D_{kt}^{m} \delta_m - c_k\right) \quad \text{for } k = 1, 2, \cdots, 61$$

- X_{it} are covariates including age, gender, education, tenure, region, year FE...
- $\bigvee y_k X_{it} \gamma > \text{interaction term of select covariates}$
- $\triangleright \sum_{m=h}^{a} D_{kt}^{m} \delta_{m}$ capture the minimum wage effects
- c_k are wage bin dummies

Great matched employer-employee data from Quadros de Pessoal

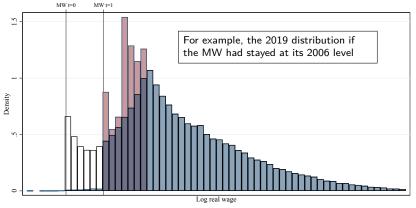
Random sample of 10% of all full-time employees in Portugal age 18-64

1986 to 2019, divided into the three periods - a specification for each period

- 1986-1994 (Importance of MW \downarrow ; Inequality \uparrow)
- 1994-2006 (Importance of MW \sim ; Inequality \sim)
- 2006-2019 (Importance of MW \uparrow ; Inequality \downarrow)

2. Constructing counterfactual distributions

Wage distribution in t = 1 if the MW had not changed since t = 0

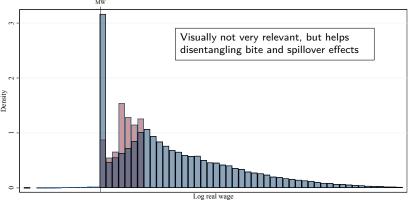


$$Prob(Y_{it} \ge y_k) = \Phi\left(X_{it}\beta + y_k X_{it}\gamma + \sum_{m=b}^{a} \frac{D_{kt}^m}{D_{kt}^m} \delta_m - c_k\right)$$

Switch the $D_{kt=1}^m$ dummies to their $\mathbf{t} = \mathbf{0}$ distribution, $D_{kt=0}^m$

2. Constructing counterfactual distributions

Wage distribution in t = 1 in the absence of spillovers



$$Prob(Y_{it} \ge y_k) = \Phi(X_{it}\beta + y_k X_{it}\gamma + \sum_{m=h}^{a} D_{kt}^{m} \delta_m - c_k)$$

Set the distribution of D_{kt}^m to 0 after the MW, $D_{kt}^m = 0$ for m > 0

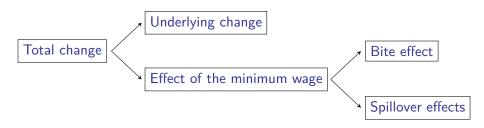
3. Quantifying and decomposing

We can **quantify** changes in the wage distribution into statistics:

- Standard deviation
- Percentile differentials
- Share of workers on the minimum wage
- Average wage

Introduction

And then **decompose** the change in those statistics:



Portugal experienced three very distinct periods

The last period, 2006-2019, is when the rising MW was most important

Mid-1980s to mid-1990s:

- $\triangle MW = 1\%$
- $\Delta 90:10 = 20\%$

Mid-1990s to mid-2000s:

- $\triangle MW = 10\%$
- \triangle Δ 90:10 = 2%

Mid-2000s to today:

- $ightharpoonup \Delta MW = 30\%$
- \triangle $\Delta 90:10 = -22\%$





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Mid-1980s to mid-1990s:

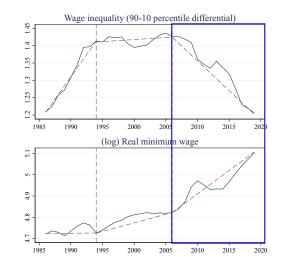
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Mid-2000s to today:

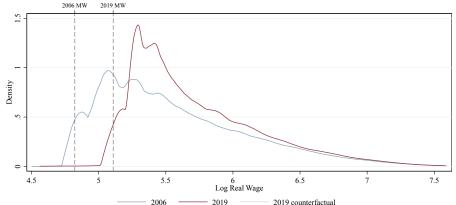
- $\triangle MW = 30\%$



The MW structurally reshaped the distribution

Had the MW not risen, the distribution would look completely different

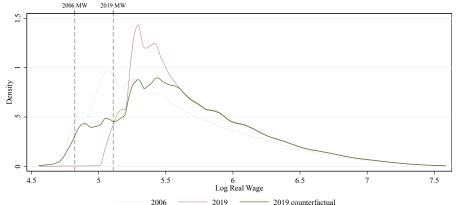
Wage distribution of 2019, had the minimum wage stayed at its 2006 level



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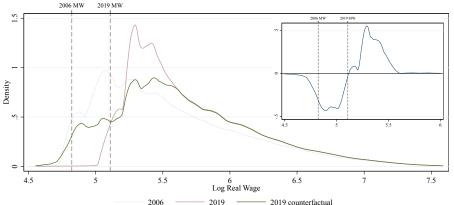
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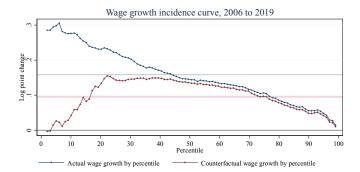




The MW fully explained the fall in wage inequality

Inequality would have remained as high as it was, had the MW not risen

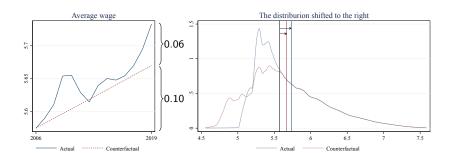
	Sd	90:10	90:50	50:10	Incidence of MW ₂₀₁₉
2006	0.58	1.43	0.95	0.48	23%
2019	0.51	1.21	0.86	0.35	4%
2019 w/ MW ₂₀₀₆	0.57	1.43	0.86	0.57	16%
Total change	-7%	-22%	-9%	-13%	-19%
Change due to MW	-6%	-22%	0%	-22%	-12%



The MW drove the average wage up

The impact of the MW was such that it shifted the distribution

The average wage grew by 16pp between 2006 and 2019. 38% of that growth (6pp) was due to the rise in the minimum wage.



Reaching very high up in the distribution, being sometimes greater than bite effects

- Spillover effects were substantial
- Reaching 40% above the minimum wage
- And in some cases being more important than the bite itself
 - ▶ E.g., most of the decrease in 50:10 was due to spillovers

	Sd	90:10	50:10	Mean
Change due to MW	-0.06	-0.22	-0.22	0.06
Change due to bite	-0.04	-0.09	-0.08	0.04
Change due to spillovers	-0.02	-0.13	-0.14	0.02

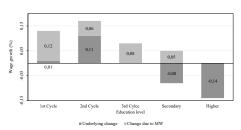
Effects were highly heterogeneous Gender

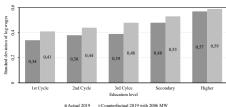
- "Within-women" inequality would have increased, had the MW not risen ("within-males" would not)
- ▶ 60% of female average wage growth was due to rising MW (only 7% for males)
- ► Cut the gender wage gap by a quarter (from 22% to 17%)

	90:10		50:1	LO	Mean wage	
	Females	Males	Females	Males	Females	Males
Total change	-0.18	-0.19	-0.09	-0.12	0.2	0.14
Underlying change	0.07	-0.09	0.14	-0.01	0.08	0.13
Change due to MW	-0.25	-0.1	-0.23	-0.09	0.12	0.01

Effects were highly heterogeneous

- Rising MW explains all wage growth for lowest educated (and none for highest)
- ► Inequality within education levels also decreased (especially for least educated)

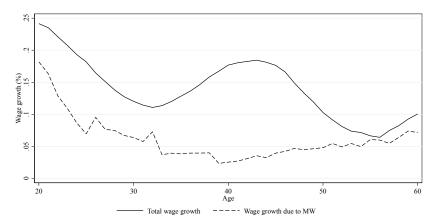




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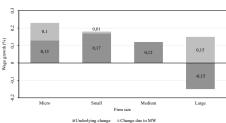
Age

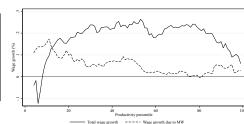
► Benefited youngest workers the most, and older workers approaching retirement



Effects were highly heterogeneous Firms

- ► Most influential for workers at micro firms and large firms
- ► And for workers at less productive firms





Conclusion

The minimum wage is definitely shaping the wage distribution

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Main results:

- Strong effects when MW rose steadily
- Structurally reshaped the distribution
- Fully explained the fall in inequality

- Drove the average wage up
- Spillovers played a crucial role
- Effects were highly heterogeneous

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Main results:

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- Drove the average wage up
- Spillovers played a crucial role
- Effects were highly heterogeneous

Further issues:

- "Pay particular attention to the role of collective bargaining. Important to discuss how this institution mediates the effects you estimate."
- "Emphasize the similarities of your setting with other European countries."
- ▶ How to incorporate disemployment effects? Maybe selection into employment (Heckman 1974, Arellano and Bonhomme 2017)